

A Block Cipher Having a Key on One Side of the Plain Text Matrix and its Inverse on the Other Side

Dr. V. U. K. Sastry¹, Prof. D. S. R. Murthy², Dr. S. Durga Bhavani³

Abstract—In this paper, we have modified the Hill cipher by developing an iterative procedure consisting of three steps. In the first step, the plain text matrix is multiplied with the key matrix on one side and with its inverse on the other side. In the second step, the plain text matrix is mixed thoroughly by using a function called Mix (). In the last step, the plain text matrix is modified by using XOR operation between the plain text matrix and the key matrix. The cryptanalysis and the avalanche effect discussed in this paper, conspicuously indicate that the cipher is a strong one and it is quite comparable with the other block ciphers.

Index Terms—Block cipher, Key, Modular arithmetic inverse, Encryption, Decryption.

I. INTRODUCTION

In a recent paper [1], we have developed a block cipher by modifying the Hill cipher. In this, we have introduced an iterative scheme, which includes the key K as a multiplier on both the sides of the plain text matrix. Here, we have adopted a procedure, in which we have used a function called Mix () for mixing the plain text at every stage of the iteration, and applied XOR operation between the plain text matrix and the key matrix. In this analysis, we have seen that the strength of the cipher is quite significant and it cannot be broken by any cryptanalytic attack.

In the present paper, our objective is to develop another modification of the Hill cipher, by including both K and K^{-1} (one on the left side and another on the right side of the plain text matrix) in encryption as well as in decryption, instead of having only K in encryption and K^{-1} in decryption. As in [1], here also we have made use of Mix () function and applied the XOR operation between the plain text matrix and the key matrix.

In section 2, we have presented the development of the cipher. We have illustrated the cipher in two different cases, and exhibited the avalanche effect in section 3. We have discussed the cryptanalysis in section 4. Finally, we have drawn conclusions in section 5.

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II. DEVELOPMENT OF THE CIPHER

Consider a plain text P which can be represented in the form of a square matrix given by

$$P = [P_{ij}], \quad i = 1 \text{ to } n, j = 1 \text{ to } n, \quad (2.1)$$

where each P_{ij} is equal to 0 or 1.

Let us choose a key k . Let it be represented in the form of a matrix given by

$$K = [K_{ij}], \quad i = 1 \text{ to } n, j = 1 \text{ to } n, \quad (2.2)$$

where each K_{ij} is a binary number.

Let

$$C = [C_{ij}], \quad i = 1 \text{ to } n, j = 1 \text{ to } n \quad (2.3)$$

be the corresponding cipher text matrix.

The process of encryption and the process of decryption adopted in this analysis are given in Fig. 1.

Here r denotes the number of rounds in the iteration process. In the process of encryption, we have the iteration scheme which includes the relations

$$P = (KPK^{-1}) \bmod 2, \quad (2.4)$$

$$P = \text{Mix}(P), \quad (2.5)$$

$$\text{and } P = P \oplus K. \quad (2.6)$$

The relation (2.4) is used to achieve diffusion, while the relations (2.5) and (2.6) are used to acquire confusion. The function $\text{Mix}(P)$ mixes the plain text at every stage of the iteration. For a detailed discussion of this function, we may refer to [1]. In the process of decryption, the function IMix represents the reverse process of Mix.

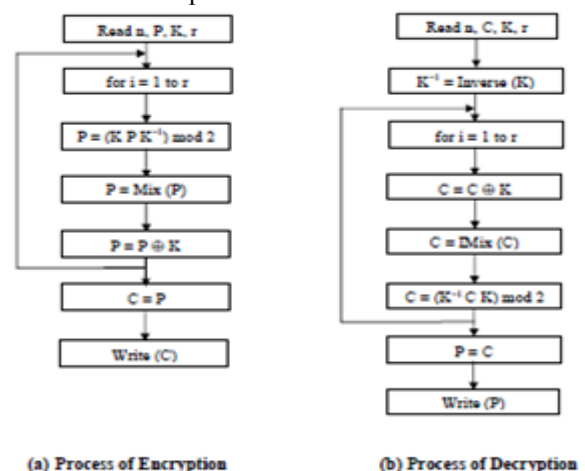


Fig. Schematic diagram of the cipher

In what follows, we present the algorithms for encryption, decryption, and for the modular arithmetic inverse of a square matrix.

Algorithm for Encryption

1. Read n, P, K, r
2. $K^{-1} = \text{Inverse}(K)$
3. for i = 1 to r
 - {
 - $P = (K P K^{-1}) \text{ mod } 2$
 - $P = \text{Mix}(P)$
 - $P = P \oplus K$
 - }
4. $C = P$
5. Write (C)

Algorithm for Decryption

1. Read n, C, K, r
2. $K^{-1} = \text{Inverse}(K)$
3. for i = 1 to r
 - {
 - $C = C \oplus K$
 - $C = \text{IMix}(C)$
 - $C = (K^{-1} C K) \text{ mod } 2$
 - }
4. $P = C$
5. Write (P)

Algorithm for Inverse (K)

// The arithmetic inverse (A^{-1}), and the determinant of the matrix (Δ) are obtained by Gauss reduction method.

1. $A = K, N = 2$
2. $A^{-1} = [A_{ij}] / \Delta, i = 1 \text{ to } n, j = 1 \text{ to } n$ // A_{ij} are the cofactors of a_{ij} , where a_{ij} are elements of A, and Δ is the determinant of A
3. for i = 1 to n
 - {
 - if $((i \Delta) \text{ mod } N = 1)$
 - $d = i;$
 - break;
 - }
4. $B = [d A_{ij}] \text{ mod } N$ // B is the modular arithmetic inverse of A

III. ILLUSTRATION OF THE CIPHER

Let us consider the following plain text.

Just now we have received the news from the border security that all the planes coming from north west corner of the country by today mid-night are containing terrorists. Shoot the planes without any second thought. Finish! (3.1)

Let us focus our attention on the first 32 characters of the above plain text. This is given by

Just now we have received the ne. (3.2)

On using the EBCDIC code, the plain text under consideration can be written in the Hexadecimal notation as follows:

D1 A4 A2 A3 40 95 96 A6 40 A6 85 40 88 81 A5 85

40 99 85 83 85 89 A5 85 84 40 A3 88 85 40 95 85. (3.3)

On placing two numbers in each row, that is, D1 A4 in the first row, A2 A3 in the second row, etc., the plain text matrix P can be written in the binary form as

$$P = \begin{pmatrix} 1 & 1 & 0 & 1 & 0 & 0 & 0 & 1 & 1 & 0 & 1 & 0 & 0 & 1 & 0 & 0 \\ 1 & 0 & 1 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 1 & 1 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 1 & 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 1 & 0 & 1 & 1 & 0 & 1 & 0 & 1 & 0 & 0 & 1 & 1 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 1 & 1 & 0 \\ 1 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 1 & 0 & 0 & 1 & 0 & 1 & 1 & 0 & 0 & 0 & 0 & 1 & 0 & 1 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 1 & 1 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 1 & 1 \\ 1 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 1 \\ 1 & 0 & 1 & 0 & 0 & 1 & 0 & 1 & 1 & 0 & 0 & 0 & 0 & 1 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 1 & 0 & 0 & 0 & 1 & 1 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 1 & 0 & 1 & 0 & 1 & 1 & 0 & 0 & 0 & 0 & 1 & 0 & 1 \end{pmatrix}$$
 (3.4)

Let us choose a key k consisting of 32 decimal numbers. Thus, we have

$$k = \begin{Bmatrix} 131 & 31 & 18 & 59 & 254 & 126 & 113 & 97 & 127 & 167 & 76 & 116 & 111 & 159 & 245 & 159 \\ 175 & 50 & 236 & 107 & 235 & 74 & 47 & 20 & 190 & 80 & 242 & 139 & 175 & 164 & 187 & 158 \end{Bmatrix}$$
 (3.5)

Then k can be written in the form of a matrix given by

$$K = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 \\ 0 & 0 & 0 & 1 & 0 & 0 & 1 & 0 & 0 & 0 & 1 & 1 & 1 & 0 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 & 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 1 \\ 0 & 1 & 1 & 1 & 0 & 0 & 0 & 1 & 0 & 1 & 1 & 0 & 0 & 0 & 0 & 1 \\ 0 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 0 & 1 & 0 & 1 & 1 & 0 & 1 & 1 \\ 0 & 1 & 0 & 0 & 1 & 1 & 0 & 0 & 0 & 1 & 1 & 1 & 0 & 1 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 & 1 & 1 & 1 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 0 & 1 & 0 & 1 & 1 & 0 & 0 & 1 & 1 & 1 & 1 & 1 \\ 1 & 0 & 1 & 0 & 1 & 1 & 1 & 1 & 0 & 0 & 0 & 1 & 1 & 0 & 0 & 1 \\ 1 & 1 & 1 & 0 & 1 & 0 & 1 & 0 & 0 & 1 & 1 & 0 & 1 & 0 & 1 & 1 \\ 1 & 1 & 1 & 0 & 1 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 1 & 0 & 1 & 0 \\ 0 & 0 & 1 & 0 & 1 & 1 & 1 & 1 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 \\ 1 & 0 & 1 & 1 & 1 & 1 & 1 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 \\ 1 & 1 & 1 & 1 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 1 & 0 & 1 & 1 \\ 1 & 0 & 1 & 0 & 1 & 1 & 1 & 1 & 1 & 0 & 1 & 0 & 0 & 0 & 1 & 0 \\ 1 & 0 & 1 & 1 & 1 & 0 & 1 & 1 & 1 & 0 & 0 & 1 & 1 & 1 & 1 & 0 \end{pmatrix}$$
 (3.6)

On using the algorithm given in section 2, the modular arithmetic inverse of K can be obtained as

$$K^{-1} = \begin{pmatrix} 0 & 1 & 0 & 1 & 0 & 1 & 1 & 0 & 0 & 1 & 0 & 1 & 1 & 0 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 & 1 & 0 & 1 & 1 & 1 & 1 & 0 & 0 & 1 & 0 & 1 \\ 0 & 0 & 0 & 1 & 1 & 1 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 0 & 0 & 1 \\ 1 & 1 & 1 & 1 & 1 & 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 & 1 & 1 & 0 & 0 & 1 & 1 & 1 & 0 & 0 & 1 & 1 & 1 \\ 1 & 0 & 1 & 0 & 1 & 1 & 0 & 0 & 0 & 1 & 1 & 0 & 0 & 1 & 1 & 1 \\ 1 & 0 & 1 & 1 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 1 & 0 & 1 & 0 \\ 0 & 0 & 1 & 1 & 0 & 1 & 0 & 1 & 0 & 1 & 0 & 1 & 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 1 & 1 & 1 & 1 \\ 0 & 0 & 0 & 1 & 1 & 0 & 0 & 1 & 1 & 1 & 0 & 0 & 1 & 0 & 0 & 0 \\ 1 & 1 & 0 & 1 & 1 & 0 & 0 & 1 & 1 & 1 & 0 & 1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 1 & 0 & 1 & 0 & 1 & 1 & 1 & 1 & 0 & 1 & 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 1 & 0 & 1 & 1 & 0 & 0 & 1 & 0 & 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 1 & 1 & 0 & 1 & 0 & 0 & 1 & 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 & 1 & 1 & 0 & 1 & 1 & 0 & 1 & 0 & 1 & 1 & 1 & 0 \end{pmatrix}$$
 (3.7)

On using (3.6) and (3.7), it can be readily shown that $K K^{-1} \text{ mod } 2 = K^{-1} K \text{ mod } 2 = I$. (3.8)

On applying the encryption algorithm, described in Section 2, we get the cipher text C in the form

$$C = \begin{pmatrix} 1 & 1 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 1 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 1 & 1 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 0 & 0 & 0 & 1 & 0 & 1 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 0 \\ 1 & 0 & 0 & 1 & 0 & 0 & 1 & 1 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 & 1 & 0 & 1 & 1 & 0 & 1 & 0 & 1 & 1 & 1 & 0 & 1 \\ 1 & 1 & 1 & 1 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 0 & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 1 & 0 & 1 \\ 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 0 & 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 1 & 1 & 1 & 0 & 1 & 0 & 1 & 1 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 1 & 1 & 1 & 1 & 0 & 0 & 0 & 1 & 1 & 0 & 1 & 0 & 0 \\ 1 & 0 & 1 & 1 & 1 & 0 & 1 & 1 & 0 & 1 & 1 & 0 & 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 1 & 0 & 1 & 0 & 0 & 1 & 0 & 1 & 1 & 0 & 1 \\ 1 & 1 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 & 0 & 0 & 1 & 1 & 0 & 0 & 1 & 1 & 1 & 0 & 0 & 0 \\ 1 & 1 & 1 & 0 & 1 & 1 & 1 & 0 & 1 & 1 & 1 & 0 & 1 & 1 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 & 1 & 0 & 1 & 0 & 0 & 1 & 0 & 1 & 0 & 1 & 1 \end{pmatrix} \quad (3.9)$$

On using (3.6), (3.7), and (3.9), and applying the decryption algorithm described in section 2, we get the Plain text P, which is the same as (3.4).

Let us now discuss the avalanche effect. Here, we modify the 11th character 'e' in (3.2) to 'd'. Then the plain text changes only in one binary bit as the EBCDIC codes of e and d are 85 and 84 respectively.

On using the modified plain text and the encryption algorithm, we get the cipher text C in the form

$$C = \begin{pmatrix} 0 & 1 & 0 & 1 & 1 & 1 & 0 & 0 & 0 & 1 & 1 & 0 & 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 1 & 0 & 1 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 1 & 1 & 1 & 0 & 1 & 0 & 0 & 1 & 1 & 1 & 0 & 1 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 1 & 0 \\ 1 & 0 & 1 & 1 & 0 & 0 & 0 & 1 & 1 & 0 & 1 & 1 & 0 & 1 & 0 & 0 \\ 1 & 1 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 1 & 1 \\ 1 & 1 & 0 & 1 & 1 & 0 & 0 & 1 & 0 & 0 & 1 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 & 1 & 1 & 0 & 1 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 1 \\ 1 & 0 & 1 & 0 & 1 & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 1 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 1 & 0 & 1 & 1 & 0 \\ 0 & 1 & 1 & 0 & 0 & 1 & 1 & 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 0 \\ 0 & 0 & 1 & 0 & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 0 & 0 \\ 1 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 0 & 1 & 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 1 & 1 & 0 & 1 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 1 & 1 & 0 & 1 & 0 & 0 & 0 & 1 \\ 1 & 1 & 1 & 1 & 1 & 0 & 0 & 1 & 1 & 0 & 0 & 0 & 1 & 1 & 0 & 1 \end{pmatrix} \quad (3.10)$$

On comparing (3.9) and (3.10), we find that the two cipher texts differ in 132 bits out of 256 bits, which is quite significant.

Now let us change the key in (3.5) by 1 binary bit. This can be achieved by replacing the 3rd element 18 of the key k by 19. Then on using the original plain text (3.4), the modified key and the encryption algorithm, we get C in the form

$$C = \begin{pmatrix} 1 & 1 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 1 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 1 & 1 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 0 & 0 & 0 & 1 & 0 & 1 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 0 \\ 1 & 0 & 0 & 1 & 0 & 0 & 1 & 1 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 & 1 & 0 & 1 & 1 & 0 & 1 & 0 & 1 & 1 & 1 & 0 & 1 \\ 1 & 1 & 1 & 1 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 0 & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 1 & 0 & 1 \\ 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 0 & 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 1 & 1 & 1 & 0 & 1 & 0 & 0 & 1 & 1 & 0 & 0 \\ 1 & 0 & 0 & 1 & 1 & 1 & 1 & 0 & 0 & 0 & 1 & 1 & 0 & 1 & 0 & 0 \\ 1 & 0 & 1 & 1 & 1 & 0 & 1 & 1 & 0 & 1 & 1 & 0 & 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 1 & 0 & 1 & 0 & 0 & 1 & 0 & 1 & 1 & 0 & 1 \\ 1 & 1 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 & 0 & 0 & 1 & 1 & 0 & 0 & 1 & 1 & 1 & 0 & 0 & 1 \\ 1 & 1 & 1 & 0 & 1 & 1 & 1 & 0 & 1 & 1 & 1 & 0 & 1 & 1 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 & 1 & 0 & 1 & 0 & 1 & 0 & 0 & 1 & 0 & 1 & 1 \end{pmatrix} \quad (3.11)$$

On comparing (3.11) with (3.9), we find that the cipher texts differ in 114 bits.

From the above analysis, we find that the Avalanche effect is quite pronounced and hence the cipher is a strong one.

By decomposing the entire plain text given by (3.1) into blocks, wherein each block is of size 32 characters, the corresponding cipher text can be written in hexadecimal notation in the form

```
C2 60 0E FF 15 FE 93 88 5B 5D F7 FF 60 85 A0 CC
2E B0 9E 34 BB 6E 15 2D C1 88 53 39 EE ED 15 4B
A4 2A 12 36 93 3F 56 53 3B 7E 00 9C 60 3B 0E D8
26 82 73 60 E7 FB 49 2C E1 52 CC 20 28 2D EA 65
79 67 F5 4D 36 EB EC 44 C1 49 8F BF 0F 31 74 64
EA A5 65 09 8B 9E D4 24 C6 6C E5 EE BC CC 50 99
E1 41 7D 0E 14 D5 31 7A A6 95 98 14 E1 C9 CC 71
08 3F 0B 29 16 62 7F B7 DA F4 CF 28 C4 58 CF FE
6C 9D DF F7 F2 F1 33 75 4B DF 33 06 8D D7 FA BA
3B 94 F6 01 8F 9E 2C 2A EC 79 A4 2F 56 DD 99 7E
A3 63 D9 B8 AA 0C 8D 07 CC 38 0C 4F EC 27 B9 8C
03 FF FA CB 69 90 A0 DD 62 55 39 F5 BF AD 66 ED
76 3B EF A2 7E 5E 29 78 7B FC DE DA 82 64 BE C3
49 D9 4B CB 9F 71 FC 5E 86 8B 04 2B 31 48 E8 3C (3.12)
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The problem under consideration can also be studied, in the case when K and K⁻¹ are interchanged, i.e., when (2.4) is replaced by

$$P = (K^{-1} P K) \text{ mod } 2. \quad (3.13)$$

This amounts to interchanging K and K⁻¹ in (2.4). Corresponding changes can be made in the algorithms. In this case, the C is given by

$$C = \begin{pmatrix} 1 & 1 & 1 & 0 & 0 & 0 & 1 & 1 & 1 & 1 & 0 & 0 & 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 1 & 0 & 1 & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 & 0 & 1 & 0 & 0 & 1 & 1 & 1 & 0 & 0 & 0 & 1 \\ 0 & 1 & 1 & 0 & 0 & 1 & 1 & 1 & 0 & 1 & 1 & 0 & 1 & 0 & 1 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 1 & 1 & 0 & 1 & 1 & 0 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 1 & 1 & 0 \\ 1 & 1 & 0 & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 0 & 0 \\ 1 & 1 & 0 & 0 & 1 & 0 & 1 & 1 & 0 & 1 & 1 & 0 & 1 & 0 & 0 & 1 \\ 1 & 1 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 1 & 1 & 0 & 1 & 0 & 1 \\ 1 & 1 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 1 & 0 & 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 0 & 0 & 1 & 1 & 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 1 & 1 & 1 & 1 & 0 & 0 & 0 & 0 \end{pmatrix} \quad (3.14)$$

Though we have got a different cipher text, on account of modifications, we have obtained the same plain text P by performing decryption.

When the plain text P is changed by one bit (i.e., the 11th character 'e' is changed to 'd'), then the corresponding cipher text assumes the form

$$C = \begin{pmatrix} 0 & 1 & 1 & 0 & 0 & 1 & 0 & 0 & 1 & 0 & 0 & 1 & 0 & 1 & 0 & 0 \\ 1 & 1 & 1 & 0 & 0 & 1 & 1 & 0 & 0 & 1 & 1 & 0 & 0 & 0 & 1 & 0 \\ 1 & 0 & 1 & 0 & 1 & 1 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 1 & 0 & 0 \\ 1 & 0 & 1 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 0 & 0 & 1 & 1 & 1 & 1 \\ 0 & 1 & 0 & 0 & 0 & 1 & 0 & 1 & 1 & 1 & 1 & 0 & 0 & 0 & 1 & 0 \\ 1 & 0 & 1 & 1 & 0 & 0 & 0 & 1 & 0 & 1 & 1 & 1 & 0 & 1 & 1 & 1 \\ 0 & 0 & 1 & 1 & 0 & 0 & 0 & 1 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 1 \\ 1 & 0 & 1 & 0 & 0 & 0 & 1 & 1 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 1 \\ 1 & 0 & 1 & 0 & 0 & 1 & 1 & 0 & 0 & 1 & 0 & 1 & 1 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 1 & 0 & 0 & 1 & 1 & 1 & 0 \\ 0 & 1 & 0 & 1 & 0 & 1 & 1 & 0 & 1 & 0 & 1 & 0 & 1 & 1 & 1 & 1 \\ 1 & 1 & 0 & 1 & 1 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 1 & 0 & 0 & 1 & 1 & 1 & 0 & 1 & 0 & 0 & 0 & 1 \\ 1 & 1 & 0 & 0 & 1 & 0 & 1 & 0 & 1 & 1 & 0 & 1 & 0 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 & 1 & 0 & 1 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 1 \end{pmatrix} \quad (3.15)$$

Thus in this case, the change in the cipher text is 133 bits out of 256 bits.

On changing 1 bit in the key (i.e., replacing 18 by 19), we have

$$C = \begin{pmatrix} 0 & 0 & 1 & 1 & 1 & 0 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 0 & 0 & 1 \\ 1 & 1 & 0 & 1 & 1 & 1 & 0 & 1 & 1 & 1 & 1 & 1 & 1 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 0 & 1 & 1 & 0 \\ 1 & 0 & 1 & 1 & 1 & 0 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 1 \\ 0 & 1 & 1 & 1 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 1 & 1 & 1 & 0 & 0 \\ 0 & 1 & 0 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 1 & 0 & 0 & 0 & 0 & 1 & 0 & 1 & 1 & 0 & 0 & 1 & 1 & 1 \\ 0 & 0 & 1 & 1 & 0 & 0 & 1 & 1 & 1 & 1 & 0 & 1 & 0 & 1 & 0 & 1 \\ 0 & 1 & 0 & 0 & 1 & 0 & 1 & 0 & 1 & 1 & 1 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 1 & 1 & 1 & 0 \\ 0 & 0 & 1 & 0 & 1 & 1 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 1 & 0 & 1 & 0 & 0 & 0 & 1 & 1 & 0 & 1 & 0 & 1 & 0 & 1 & 1 \\ 0 & 1 & 1 & 0 & 0 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 1 & 0 & 1 & 1 & 0 & 1 & 1 & 0 & 0 & 1 & 1 & 0 & 1 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 & 1 & 1 & 0 & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \quad (3.16)$$

From (3.14) and (3.16), we notice the change in C is 123 bits out of 256 bits. From the above analysis, we find that the Avalanche effect is quite significant and hence this cipher is also a very strong one.

In this case, the cipher text corresponding to the entire plain text (3.1), in hexadecimal form, is given by

```
E3 C2 96 02 68 21 12 71 73 B5 23 68 54 56 B6 AB
16 D0 64 AD D8 2B 58 0C CB 33 C2 AA 1F 36 08 F8
44 10 72 F8 CF D6 9B B1 3A 95 BC A0 4A 85 B8 81
19 98 64 BB 83 70 67 5B 07 D5 15 9C 63 8C 9C CC
84 F4 E8 12 2B DB 50 87 63 A4 A0 34 68 DD B9 CC
0A FE D0 80 EC 61 86 49 6C FC C8 B5 DD 8E AD B5
82 5B CA E6 CB E7 91 2F FF 5C D5 B1 7B 25 62 5B
47 B1 98 B6 29 E5 52 C7 1D 44 D9 CF D0 DC 05 40
8D D4 FB F9 A6 66 D7 4E 25 68 7E 52 8A 9A 6D D7
D0 46 7C FF A6 23 AA 5D 37 C8 22 A1 B7 53 06 6A
79 5E 7D 86 1C 33 5E C6 15 05 23 54 C2 8C A9 F3
A1 4A 1B F9 25 96 B5 DE C1 64 CD 27 65 6F EA 1A
97 18 7B BC EA 88 3E 79 BE C4 10 06 D0 5D 4E 66
77 ED 17 DD 2A BE 53 64 9E 95 CD 87 4A CB 36 39 (3.17)
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IV. CRYPTANALYSIS

The different types of cryptanalytical attacks available in the literature are:

- (1) Cipher text only attack,
- (2) Known plain text attack,
- (3) Chosen plain text attack,
- (4) Chosen cipher text attack.

When the cipher text is known to us, we can determine the plain text, if the key is known. As the key contains 32 decimal numbers, the key space is of size

$$2^{256} = (10^3)^{256} = 10^{768}$$

As the computation of the cipher text corresponding to all possible keys would take a very large amount of time, the cipher cannot be broken by the brute force approach.

We know that, the Hill cipher can be broken by the known plain text attack, as we can form a direct relation between C and P. But in the present modification, which involves K and K^{-1} , one on the left side of P and the other on the right side of P, and the process of iteration together with the Mix function and the XOR operation, we cannot get a direct relation between C and P. Hence, this cipher developed in this analysis cannot be broken by the known plain text attack.

The chosen plain / cipher text attack is totally ruled out as the steps involved in the cipher are typical in nature.

V. CONCLUSIONS

In this paper, we have modified the Hill cipher, governed by the single relation

$$C = (K P) \bmod 26, \quad (5.1)$$

in two different cases.

In case one, the iterative scheme includes the relations

$$P = (K P K^{-1}) \bmod 26, \quad (5.2)$$

$$P = \text{Mix}(P), \quad (5.3)$$

$$\text{and } P = P \oplus K, \quad (5.4)$$

and in case two, it includes the relations

$$P = (K^{-1} P K) \bmod 26, \quad (5.5)$$

$$P = \text{Mix}(P), \quad (5.6)$$

$$\text{and } P = P \oplus K. \quad (5.7)$$

In this analysis, the length of the plain text block is 256 bits and the length of the cipher text block is also 256 bits. As the cryptanalysis clearly indicates, this cipher is a strong one and

it cannot be broken by any cryptanalytic attack. This analysis can be extended to a block of any size by using the concept of interlacing [2].

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