

# Secure Remote Data Processing in Cloud Computing

Mohd Rizuan Baharon, Qi Shi, David Llewellyn-Jones, and Madij Merabti

**Abstract**—Cloud computing provides solutions as a service to meet customers' needs such as massive data storage and a lot of computing resources to process customer data efficiently. To fully utilize such services, data need to be outsourced to Cloud Service Providers (CSPs). However, outsourcing precious data to the CSPs could lead to a disaster. Thus, the data need to be protected by means of encryption techniques. Primitive encryption techniques are ineffective to be used as such techniques required decryption process. To overcome such a problem, a fully homomorphic encryption (FHE) scheme is needed as the scheme enables encrypted data to be processed in an encrypted form. There are a number of existing FHE schemes have been proposed and improved upon, but efficiency is still a big obstacle for their implementation. Thus, in this paper, a new fully homomorphic encryption scheme based on finite fields that supports an  $n$ -multilinear map is proposed. The scheme should support the  $n$ -multilinear map so as to allow for arbitrary multiplications on encrypted data. Moreover, a new protocol that enables three or more parties to communicate with one another to process data in an encrypted form is proposed in this paper.

**Index Terms**—Cloud computing, elliptic curve groups, homomorphic encryption,  $n$ -multilinear map.

## I. INTRODUCTION

Processing data remotely is becoming a hot trend for people to deal with their data recently. This is due to the benefits offered by the advent technology of cloud computing. Cloud Services Providers (CSPs) provide solutions as a service to meet customers' needs such as massive storage spaces and powerful computing resources to store and process their data efficiently. An example of services that provided by the CSPs like HP, is a rendering service. DreamWorks for instance has leveraged services from HP to access a big amount of computing resources to generate 3D frame. HP Media Cloud Solutions have been used to help them to produce animated films like Shrek and Toy Story. Such films require a lot of computing resources for its creation. Thus, the leverage services provided by CSPs enable animated film studios to reduce their upfront costs for servers and manpower as their services are charged on a utility basis [1].

To fully utilize services provided by the CSPs, data need to be outsourced into the CSPs. However, outsourcing precious data to an untrusted third party like a CSP could

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lead to data disclosure or data misuse by the CSP [2]. Thus, such data need to be protected by means of encryption techniques. Primitive encryption technique like AES is ideal to be used for storage purposes as this encryption technique provides a strong protection to the data in the cloud storage [3]. However, to enable the CSP to process the data, the associated decryption technique needs to be applied first to decrypt the encrypted data. The decryption in the cloud environment by the CSP is not a wise option as it may disclose some sensitive content of the data to the CSP. Furthermore, decrypting in such a way probably could disclose the data to other cloud customers as vulnerabilities exist in the environment [4]. Thus, to enable data to be processed securely in such an environment, a fully homomorphic encryption scheme is believed to be one of the potential solutions as such a scheme allows data to be processed in an encrypted form [5].

Recently, a number of existing fully homomorphic encryption schemes based on Lattices have been proposed and improved upon. Nevertheless, all of them are far from practical as efficiency is still a big obstacle for their implementation. This is due to the amount of noise used at encryption level for security reasons [6]. Managing noise on encrypted data is not an easy task mainly because the process involves many operations such as those in a rendering equation. Typically, the noise is doubled during addition, while increasing exponentially during multiplication [7]. Using a 2D/3D frame as an example, a rendering equation is used to create the frame based on a scene or model. The equation involves additions and multiplications on an input data. To enable some encrypted data to be processed using such an equation efficiently, an encryption technique, which enables arbitrary additions and multiplications with less noise to be performed on the encrypted data, is needed. Such an encryption technique is highly required to allow the data to be rendered by cloud-based applications to produce the 2D/3D frame in the cloud environment.

Additionally, a scheme proposed by Boneh *et al.* [8], which supports a bilinear map, has a limitation as the scheme allows arbitrary additions but just one multiplication on encrypted data. Such a scheme needs to be improved as the scheme is unable to run a process that involves more than one multiplication on encrypted data. Due to such a limitation, a new fully homomorphic encryption scheme based on a finite field that supports an  $n$ -multilinear map is proposed in this paper. The scheme supports the  $n$ -multilinear map so as to allow for arbitrary multiplications on encrypted data. Furthermore, a suitable protocol is required to allow a process to be executed by a designated CSP. Thus, a new secure protocol is also proposed in this paper. The protocol enables three or more parties to communicate with one another to get a result of processed data in an encrypted form.

This paper is structured as follows. Section II describes the

contributions of the paper. Some essential concepts used in this paper are summarised in Section III. In Section IV, explanations of some analysis, discussion and preliminaries results will be given. Finally, a conclusion of this paper is provided in Section V.

## II. PAPER CONTRIBUTION

The expected key contributions of this paper are summarised in the following points:

- 1) A new FHE scheme. A new FHE scheme based on a finite field that supports an  $n$ -multilinear map is proposed. An elliptic curve EC group is implemented as the underlying group as EC promises high efficiency and strong security. Previous work that supports a bilinear map allows arbitrary additions but only one multiplication. Thus, to achieve arbitrary multiplications on encrypted data, an  $n$ -multilinear map will be implemented to the scheme subject to the existence of the generator in the map.
- 2) A secure data processing protocol. The protocol uses the above proposed FHE scheme to enable a huge amount of sensitive data to be processed securely and efficiently.

## III. BACKGROUND

This section describes several fundamental concepts and definitions that have been used in the proposed scheme.

### A. An $n$ -Multilinear Map

*Definition of  $n$ -Multilinear Map: [9]*

Let  $G_1, G_2, \dots, G_n$  and  $G_t$  be cyclic groups of the same prime order  $q$  and  $\mathbb{Z}_q^*$  be a finite field that is closed under multiplication operation.  $n$ -multilinear groups  $G = G_1 = G_2 = \dots = G_n$  are all isomorphic to one another as they have the same order and are cyclic. An  $n$ -multilinear map is a function  $e: G_1 \times G_2 \times \dots \times G_n \rightarrow G_t$  such that the following properties are satisfied:

- 1) For all  $a_1, a_2, \dots, a_n \in \mathbb{Z}_q^*$  and  $g_1, g_2, \dots, g_n \in G$ ,  $e(g_1^{a_1}, g_2^{a_2}, \dots, g_n^{a_n}) = e(g_1, g_2, \dots, g_n)^{a_1 a_2 \dots a_n} \in G_t$ .
- 2) The map is non-degenerate: If  $g \in G$  generates  $G$  then  $e(g, g, \dots, g) \in G_t$  generates  $G_t$ .

An example of the construction of  $n$ -multilinear groups of order  $n$  using the Elliptic Curve group is given as below.

An  $n$ -multilinear group  $G = G_1 = G_2 = \dots = G_n$  of order  $n$  can be constructed as follows:

- 1) Let  $l = 2$ , and  $n = 10$  such that  $n$  is a square-free integer that is not divisible by 3. A square-free integer is one divisible by no square number, except 1. Then,  $q = ln - 1 = 2(10) - 1 = 19$ .
- 2) Let  $E_{(1,0)}(F_{19})$ :  $y^2 = x^3 + x$  defined over a finite field  $F_{19}$  be the group of points. The curve has  $q + 1 = ln = 20$  points in  $F_{19}$ . Thus, there exists a subgroup  $G$  in  $E_{(1,0)}(F_{19})$  of order 10 since  $n = 10$ .
- 3) Let  $G_t$  be the subgroup of a finite field that is closed under multiplication,  $F_{19^2}^* = F_{361}^*$  of order  $n$ . Our aim is to have an  $n$ -multilinear map  $e: G_1 \times G_2 \times \dots \times G_n \rightarrow G_t$  which includes the admissible  $n$ -multilinear map generator.

### B. Elliptic Curve over Finite Field $F_q$

Let  $q > 3$  be an odd prime. An EC  $E$  over a prime field  $F_q$  is defined by an equation of the form:

$$y^2 = x^3 + ax + b$$

where  $a, b \in F_q$ , and  $4a^3 + 27b^2 \not\equiv 0 \pmod{q}$ .

The set  $E(F_q)$  consists of all points  $(x, y), x \in F_q$ , which satisfy the above equation, together with the point at infinity  $O$ . The addition of distinct points and doubling a point on the curve can be done through the following algebraic formula. Let  $P, Q, O$ , and  $R$  be points on a curve  $E(F_q)$ . Then,

- 1)  $P + O = O + P = P$  For all  $P \in E(F_q)$ .
- 2) If  $P = (x, y) \in E(F_q)$ , then  $(x, y) + (x, -y) = O$ . (The point  $(x, -y)$  is denoted by  $-P$ , and is called the negative of  $P$ ).
- 3) (Point addition) Let  $P = (x_1, y_1) \in E(F_q)$  and  $Q = (x_2, y_2) \in E(F_q)$  where  $P \neq \pm Q$ . Then  $P + Q = R = (x_3, y_3)$ , where  $x_3 = \left(\frac{y_2 - y_1}{x_2 - x_1}\right)^2 - x_1 - x_2$  and  $y_3 = \left(\frac{y_2 - y_1}{x_2 - x_1}\right)(x_1 - x_3) - y_1$ .
- 4) (Point doubling) Let  $P = (x_1, y_1) \in E(F_q)$ , where  $P \neq -P$ . Then  $2P = (x_3, y_3)$ , where  $x_3 = \left(\frac{3x_1^2 + a}{2y_1}\right)^2 - 2x_1$  and  $y_3 = \left(\frac{3x_1^2 + a}{2y_1}\right)(x_1 - x_3) - y_1$ .

### C. Working Example:

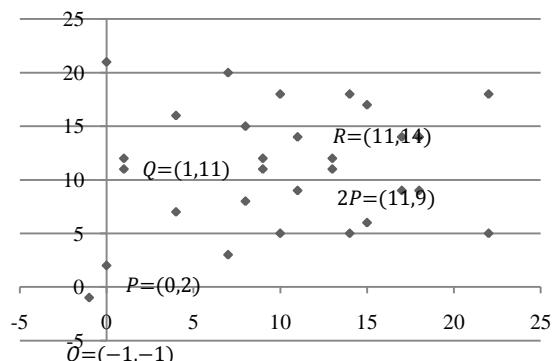


Fig. 1. Elliptic curve group over  $F_{23}$ ,  $E(F_{23})$ .

Point addition and doubling can be computed as below, where the results of computation are as illustrated in Fig. 1.

- 1) Point Addition

Let  $P = (0, 2)$  and  $Q = (1, 11) \in E_{(1,4)}(F_{23})$  where  $P \neq \pm Q$ . Then  $P + Q = R = (x_3, y_3)$ , where  $x_3 = \left(\frac{11-2}{1-0}\right)^2 - 0 - 1 = 11$ ,  $y_3 = \left(\frac{11-2}{1-0}\right)(0 - 11) - 2 = 14$ . Thus,  $R = (11, 14) \in E_{(1,4)}(F_{23})$ .

- 2) Point Doubling

Let  $P = (0, 2) \in E_{(1,4)}(F_{23})$ , where  $P \neq -P$ . Then  $2P = (x_3, y_3)$ , where  $x_3 = \left(\frac{3(0)^2 + 1}{2(2)}\right)^2 - 2(0) = 11$ ,  $y_3 = \left(\frac{3(0)^2 + 1}{2(2)}\right)(0 - 11) - 2 = 9$ . Thus,  $2P = (11, 9) \in E_{(1,4)}(F_{23})$ .

#### IV. THE PROPOSED SCHEME AND PROTOCOL

This section describes the proposed scheme and its related processes. This section also provides the proposed protocol together with its descriptions.

##### A. The Proposed Scheme

Let  $m \in \{0,1\}$  be a plaintext,  $c$  be a ciphertext,  $g \in G$  be a generator of  $G$ ,  $r \in \mathbb{Z}$ , and  $h = g^{\alpha q_2}$  such that  $\alpha$ , and  $q_2 \in \mathbb{Z}$ . Then

- 1) Encryption:  $c(m) = g^m h^r$ .
- 2) Decryption:  $m = c^{-1}(c(m)) = \log_{g^{q_1}} c^{q_1}(m) = \log_{g^{q_1}}(g^m h^r)^{q_1} = \log_{g^{q_1}}(g^{q_1})^m$ .

##### B. Scheme Requirements

The scheme should hold such properties:

1. Homomorphic under  $*$  operations.

- $C = \sum_{i=1}^n c_i = \prod_{i=1}^n c_i h^r$  is homomorphic under addition.
- $C = \prod_{i=1}^n c_i$  is homomorphic under multiplication.

2. Double layer encryption.

To ensure the privacy of the outsource data is preserved.

##### C. Basic Description Protocol

The protocol is illustrated in Fig. 2, and its steps are explained below.

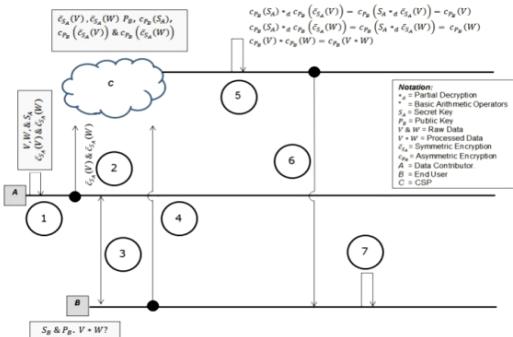


Fig. 2. The protocol.

- 1) A creates raw data  $V = v_i \in \{0,1\}$ ,  $W = w_i \in \{0,1\}$  for  $i = 1, 2, \dots, n$  and secret key  $S_A$ . Then, A encrypts  $V$  and  $W$  using  $S_A$ .
- 2) A sends  $\bar{c}_{S_A}(V)$  and  $\bar{c}_{S_A}(W)$  to C.
- 3) A encrypts  $S_A$  using  $P_B$ . A sends  $c_{P_B}(S_A)$  to B to enable B to decrypt the processed result.
- 4) B requests C to re-encrypt  $\bar{c}_{S_A}(V)$  and  $\bar{c}_{S_A}(W)$  using  $P_B$ . Then, B sends  $c_{P_B}(S_A)$  and instructions to C for processing on  $c_{P_B}(\bar{c}_{S_A}(V))$  and  $c_{P_B}(\bar{c}_{S_A}(W))$ .
- 5) C re-encrypts  $\bar{c}_{S_A}(V)$  and  $\bar{c}_{S_A}(W)$  using  $P_B$  and run processes called partial decryption process:
 
$$c_{P_B}(S_A) *_d c_{P_B}(\bar{c}_{S_A}(V)) = c_{P_B}(S_A *_d \bar{c}_{S_A}(V)) = c_{P_B}(V).$$

$$c_{P_B}(S_A) *_d c_{P_B}(\bar{c}_{S_A}(W)) = c_{P_B}(S_A *_d \bar{c}_{S_A}(W)) = c_{P_B}(W).$$

*Definition of  $*_d$ :*

Let  $a$  and  $b$  be integers such that  $a$  is a secret key to encrypt  $x$  and  $b = c_a(x)$  is a ciphertext. Then,  $a *_d b = c_a^{-1}(b) = x$ .

Then, the process on  $c_{P_B}(V)$  and  $c_{P_B}(W)$  is executed to produce  $c_{P_B}(V * W)$ .

- 1) C sends the result  $c_{P_B}(V * W)$  to B.
- 2) B decrypts the result using  $S_B$  to recover  $V * W$ .

#### V. THE PRELIMINARY RESULTS

The preliminary results based on performance of the encryption/decryption process proposed in the previous section have been summarised in Table I.

TABLE I: PERFORMANCE ANALYSIS OF ENCRYPTION/DECRYPTION PROCESS

Performer	Tasks	Method	Performance	Descriptions/Results
A	Encrypts raw data ( $V$ and $W$ ) using $S_A$	Symmetric encryption scheme	Fast	$\bar{c}_{S_A}(V)$ , and $\bar{c}_{S_A}(W)$
	Encrypts $S_A$ using $P_B$	The proposed scheme /asymmetric	Fast	The key size is short. $c_{P_B}(S_A)$ .
B	Decrypts $c_{P_B}(S_A)$ using $S_B$ .	The proposed scheme /asymmetric	Fast	The key size is short. $d_{S_B}(c_{P_B}(S_A)) = S_A$ .
	Decrypts $c_{P_B}(V * W)$ using $S_B$		Fast/Slow	It is depends on the size of the output. $V * W$ .
C	Re-encrypts $\bar{c}_{S_A}(V)$ , and $\bar{c}_{S_A}(W)$ using $P_B$	The proposed scheme /asymmetric	Fast	$c_{P_B}(\bar{c}_{S_A}(V))$ , and $c_{P_B}(\bar{c}_{S_A}(W))$
	Run a partial decryption process		Fast	$c_{P_B}(S_A) *_d c_{P_B}(\bar{c}_{S_A}(V)) = c_{P_B}(S_A *_d \bar{c}_{S_A}(V)) = c_{P_B}(V).$ $c_{P_B}(S_A) *_d c_{P_B}(\bar{c}_{S_A}(W)) = c_{P_B}(S_A *_d \bar{c}_{S_A}(W)) = c_{P_B}(W).$

#### VI. CONCLUSION

A new FHE scheme for processing remote data in an encrypted form has been proposed in this paper. The EC group is implemented as the underlying group due to EC's promising efficiency, and also an  $n$ -multilinear map should be supported by the scheme to achieve the fully homomorphic properties. The proposed scheme is implemented in a process that requires arbitrary additions and multiplications such as a rendering process to check the ability of the proposed scheme to compute arbitrary additions and multiplications on encrypted data. The security of data encrypted and processed using the proposed protocol is guaranteed in cloud environments due to no information disclosed at any stage. Further works of this paper will be looking at the generator of an  $n$ -multilinear map. Furthermore, various ways will be investigated to prove that the generator exists in the map and can be computed efficiently.

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