

# Force Signal Tuning for a Surgical Robotic Arm Using PID Controller

Gamal I. Selim, Noha H. El- Amary, and Dina M. Aboul Dahab

**Abstract**—In this paper, the modeling, control and simulation of a robotic arm is presented. The goal of the controller is to improve and adjust the output force of the arm using Proportional Integral Differential (PID) controllers. Lately the application of robotics in the field of surgery has opened fields of research that has helped ensure the accuracy, durability, dexterity and the ability for repetition. The combination of the human surgeon's judgmental capabilities with these aforementioned characteristics proves to be an interestingly challenging duo/encounter. The studied system is simulated to consist of the equations of the dynamic motion of the robotic arm with the controller participation. Using the concept of force balance between the surgical robotic arm and the organ, PID controllers are added to smoothen and to slow down the output impact force of the robot in all dimensions. The system is investigated without any control system, with PI controller and PID controller. Different gain values for PID controllers are studied. Output obtained from the simulation show satisfactory response.

**Index Terms**—Surgical robotic arm, force balance concept, force signal tuning, PID controller effect.

## I. INTRODUCTION

Robotics surgery begins to lead the way in the surgical profession with the emerge of advanced and more helpful technology. Surgical robotic devices are classified into: (1) large, high precision robots (image guided or tele-operated), (2) handheld smart medical tools and (3) miniature endoscopic robots. Minimally Invasive Surgery (MIS) is an operation technique established in the 1980s. It differs from open surgery in that the surgeon works with long instruments through small incisions (typically < 10mm) and that he has no direct access to the operation field as in open surgery. It's mentioned that robotic surgery is preferred in MIS for its dexterity, precision and repeatability. For tele-operated robots, it focuses on two examples: the "Da Vinci Surgical System" and the "Zeus" dexterous tele-operated system. An intelligent hand-held instrument and the mechatronic arthroscope for the medical tools are used. Two examples for the endoscopic robots are given namely, the inchworm colonoscopy prototype and the miniaturized system [1]. Three basic disadvantages for the MIS include: (1) due to the indirect surgeon's access to the operating field, the tissues cannot be palpated anymore, (2) the appearing contact force between instrument and tissue can hardly be sensed and (3)

direct hand-eye coordinate is lost as the instrument has to be moved around an invariant fulcrum point intuitive using only four degrees of freedom (DOFs) whilst remaining inside the body of the patient due to the kinematic restrictions. Therefore, the surgeon cannot reach any point in the work space at an arbitrary orientation [2]. A tele-operator that supports manipulators in 4 DOFs in the patient and provides visual and haptic sensor is classified in [3]. Reference [4] explains the effect of varying degrees of freedom of force feedback on the performance of manipulation task using a tele-operation system. An experimental evaluation of the role of force feedback in blunt dissection (one of the surgical manipulation tasks employed in minimally invasive surgery) has been carried out [5], [6]. A central scheme for augmented co-manipulation with force feedback is presented where a second force sensor has been found necessary to distinguish manipulator and environmental forces in addition to modifying torques [7]. The development of actuated and sensorized instruments for minimally invasive robotic surgery which are a necessary prerequisite for haptic feedback is developed [8]. In reference [9] a 5mm diameter triaxial force sensor has been developed for MIS which measures three force components. The design, implementation and testing for a miniature force sensor developed to measure forces in three dimensions at the tip of a microsurgical instrument is tackled [10]. Reference [11] proposes a model-based controller to correct the command motions where the thin instruments flexion introduces errors into models of the robot kinematics.

Proportional Integral Differential (PID) controller constitutes the most widely used type of feedback. A percentage of more than 90% of the controllers used in the process industries are PID controllers and advanced versions of the PID as proven by an investigation carried out in Japan in 1989. The proportional control action is based on the current value of the control error while the integral control action is based on the past values of the control error. On the other hand, the differential control action is based on the predicted future values of the control error [12]. In this paper, a control system is developed to adjust the output reached force of the robotic arm.

## II. DYNAMIC MODEL OF A ROBOTIC ARM

A Robotic arm which is used in surgical operation is shown in fig. (1), (2). It consists of two links, a static link and a dynamic link. The junction between the two links has three degrees of freedom represented in the variable of motions  $q_1$ ,  $q_2$ , and  $q_3$ .

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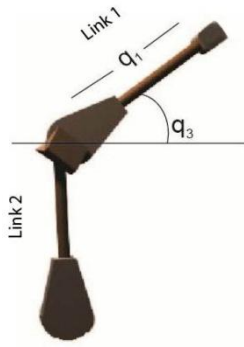


Fig. 1. A side view of the robotic arm

The mathematical model of the dynamic link of the robotic arm is given by the following equations using Lagrange equation [13].

$$\ddot{q}_1 = \frac{1}{m}(u_1 \cos q_3^2 + (u_2 - m\dot{q}_1\dot{q}_3) \cos q_3 \sin q_3 - \dot{q}_2\dot{q}_3 \sin q_3^2) \quad (1)$$

$$\ddot{q}_2 = \frac{1}{m}(u_2 \sin q_3^2 + (u_1 + m\dot{q}_2\dot{q}_3) \cos q_3 \sin q_3 + \dot{q}_1\dot{q}_3 \cos q_3^2) \quad (2)$$

$$\ddot{q}_3 = \frac{u_3}{I} \quad (3)$$

where;

$q_1$  denotes the elongation of the arm,  $q_2$  denotes the heading direction,  $q_3$  denotes angle with  $q_2$  plane ( $0 < q_3 < \pi/2$ ),  $M$  is the mass of the robotic arm,  $I$  is the robotic arm inertia about the axis of rotation,  $(u_1, u_2)$  are the forces along the  $(q_1, q_2)$  directions and  $u_3$  is the torque about an axis through the contact point and orthogonal to the plane. These equations are derived from Lagrange equation to get:

$$u_1 = m\ddot{q}_1 - \lambda \sin q_3 \quad (4)$$

$$u_2 = m\ddot{q}_2 + \lambda \cos q_3 \quad (5)$$

$$u_3 = I\ddot{q}_3 \quad (6)$$

where;

$\lambda$  is the Lagrange multiplier, by applying the velocity constraint

$$\dot{q}_1 \sin q_3 - \dot{q}_2 \cos q_3 = 0 \quad (7)$$

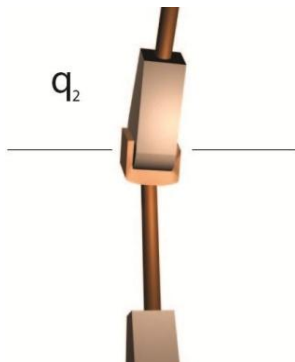


Fig. 2. A front view for the robotic arm

Differentiating this constraint, we get

$$\dot{q}_1 \sin q_3 + \dot{q}_1\dot{q}_3 \cos q_3 - \dot{q}_2 \cos q_3 + \dot{q}_2\dot{q}_3 \sin q_3 = 0 \quad (8)$$

Solving equation (6) and (8), we get

$$\lambda = (u_2 - m\dot{q}_1\dot{q}_3) \cos q_3 - (u_1 + m\dot{q}_2\dot{q}_3) \sin q_3 \quad (9)$$

### III. CONTROL SCHEME

A developed control system is designed to control the output force signal of the robotic arm. The control system depends on the force balance concept between the organ and the robotic arm. The system response is evaluated before and after inserting the controller. The controller design is evaluated using a PI and a PID controller and the results are investigated. A general representation for the whole system of the robotic arm with its controller is shown in fig.3. A part of the simulated system on the Simulink is clarified in fig. 4. The input per unit predetermined force signal from the organ (reference signal) and the output feedback signal of the forces are marked in fig. 4.

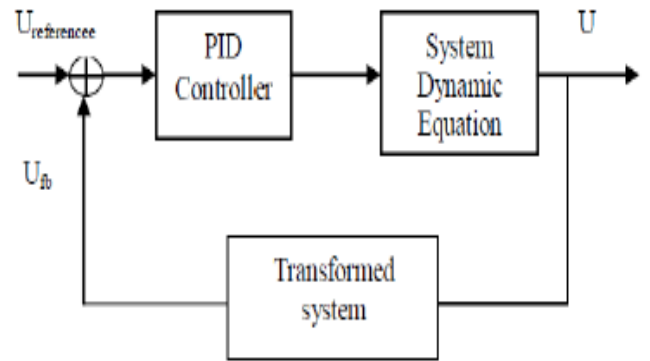


Fig. 3. System representation for the whole system of the robotic arm

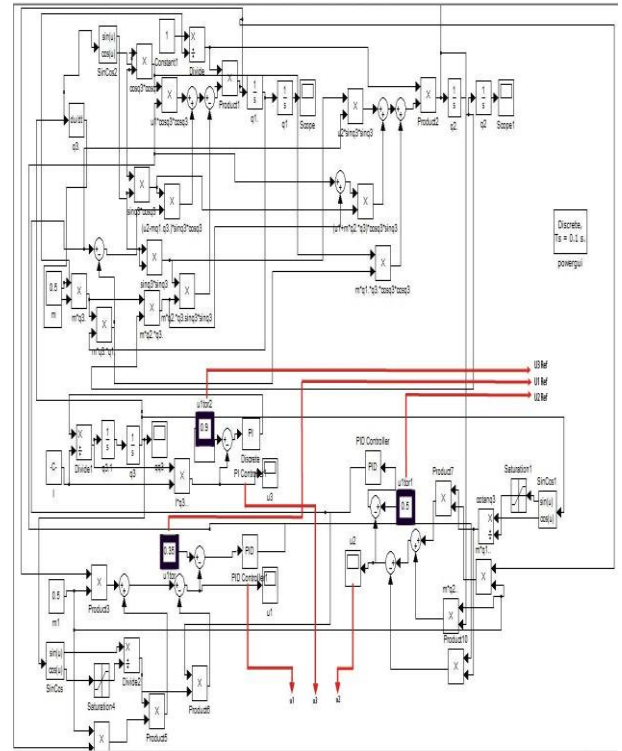


Fig. 4. A part of the Simulink for the simulated robotic arm

### IV. TUNED FORCE SIGNAL RESULTS

After simulating the studied system on the Simulink, the output force results of the system is clarified as follows. The

responses of the output force  $u_1$  are shown in fig. 5, fig. 6, fig. 7, fig. 8. All the diagrams show the variation of the output force from the robotic with time. Fig.5 represents the response of the system without any controller. The output force for the organ with time isn't reached. Some oscillations appeared after  $t=65$ seconds that became greater with time without halting (unstable case).

When PI controller is used as shown in fig. 6, the output force reaches the required reference signal but with an unacceptable oscillatory behavior as in the case before. An observable improvement (as illustrated in fig. 7) appears when a PID controller is applied though with some oscillations and a 10% maximum overshoot which is however unacceptable for a surgical robot. When the proportional gain is adjusted, the robotic arm reaches a smooth output force signal as shown in fig.8. The output force  $u_2$  is shown in fig. 9, fig. 10, fig. 11, fig. 12. A trial is carried out in the beginning without a controller which results in a quick exponential rising of  $u_2$  with time as shown in fig.9. A noted overshoot occurs when a PI controller is applied which is unacceptable in robotic surgery as in fig. 10. By applying the PID controller, the output force reaches the required reference signal, but with the unacceptable oscillatory behavior as in the previous case (as illustrated in fig. 11). With some tuning applied, fig. 12 clarifies an acceptable smooth response for the output force. Fig. 13, fig. 14 represents the output force response  $u_3$  in the absence of any controllers and in the presence of a PI controller respectively. A result below the required was noticed in the former and more acceptable one in latter.

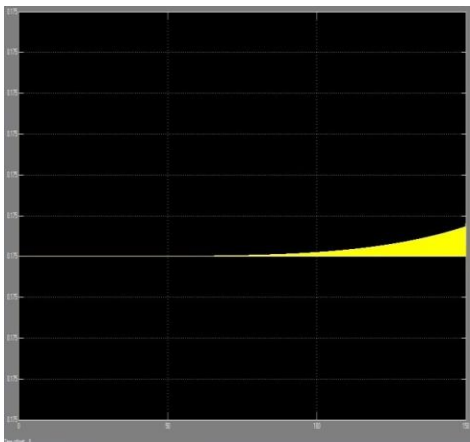


Fig. 5. The force  $u_1$  versus time without applying PID controller

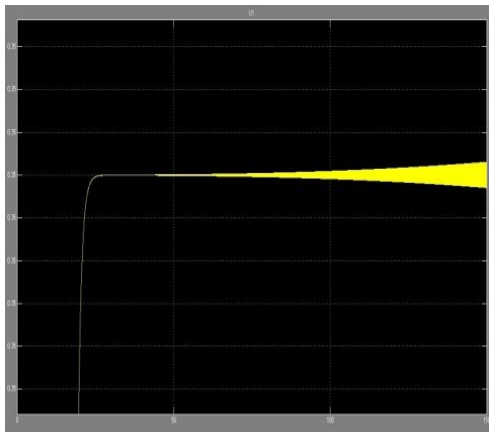


Fig. 6. The force  $u_1$  versus time after applying PI controller ( $K_p=0.1, K_i=1$ )

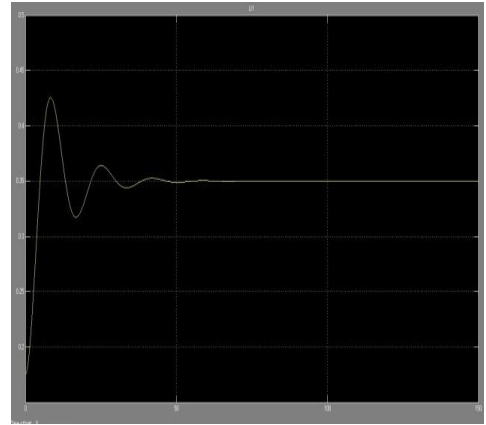


Fig. 7. The force  $u_1$  versus time after applying PID controller ( $K_p=1, K_i=1.5, K_d=10$ )

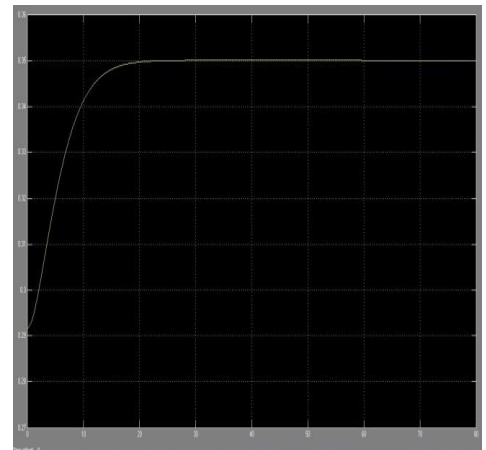


Fig. 8. The force  $u_1$  versus time after applying PID controller ( $K_p=5, K_i=1, K_d=10$ )

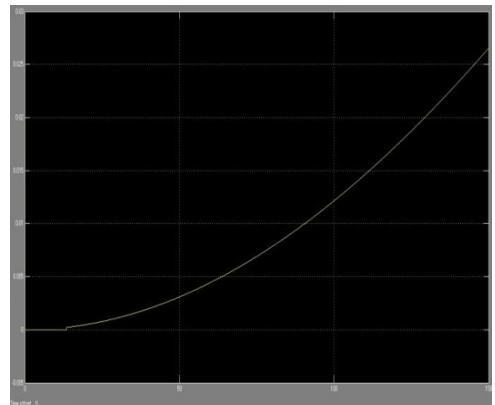


Fig. 9. The force  $u_2$  versus time without applying PID controller

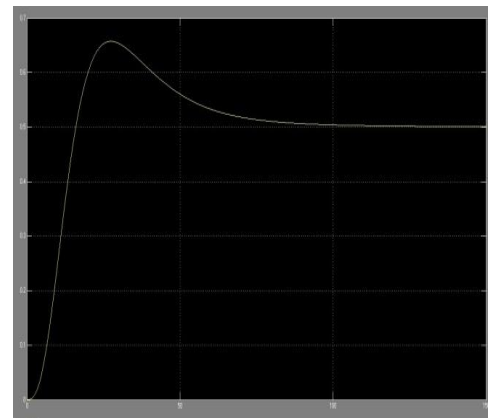


Fig. 10. The force  $u_2$  versus time after applying PI controller ( $K_p=1000, k_i=100$ )

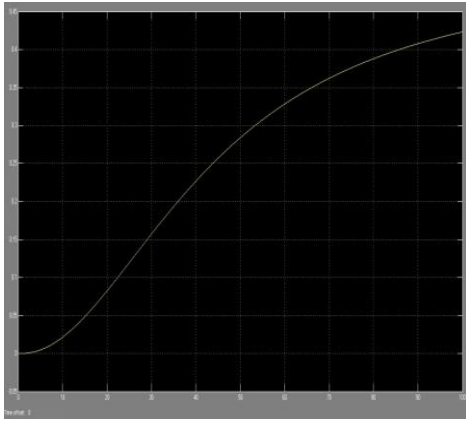


Fig. 11. The force  $u_2$  versus time after applying PID controller ( $K_p=120, K_i=0.01, K_d=1$ )

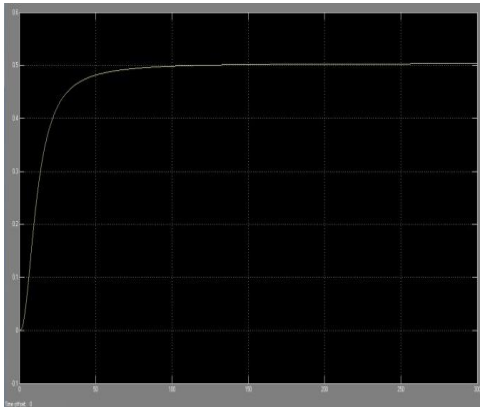


Fig. 12. The force  $u_2$  versus time after applying PID controller ( $K_p=2000, K_i=1, K_d=1000$ )

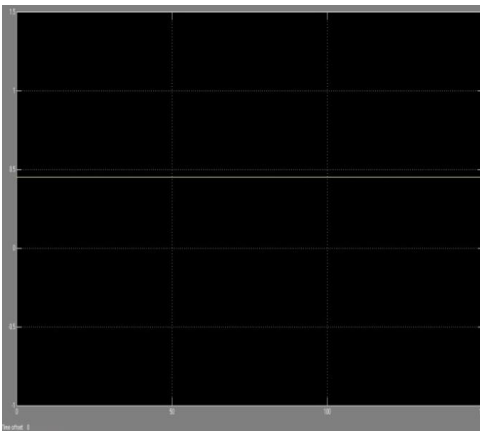


Fig. 13. The force  $u_3$  versus time without applying PI controller

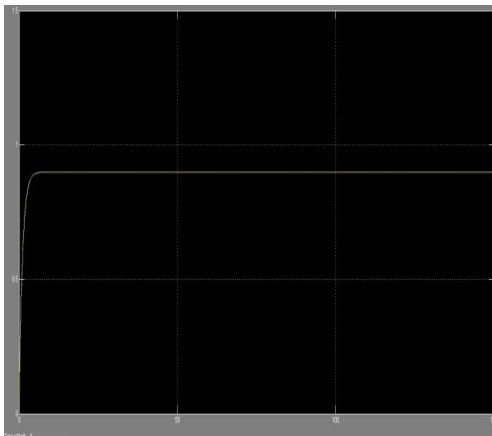


Fig. 14. The force  $u_3$  versus time after applying PI controller ( $K_p=0.1, K_i=1$ )

## V. CONCLUSION

Tuning of output force from a robotic arm which is used in robotic surgery is presented in this paper. The robotic arm dynamic is simulated and investigated at the junction between robot arm links utilizing simulink. The arm consists of two links. The three dimensions forces of the dynamic link are studied. The target is to produce a smooth and relatively slow force reaction from the robotic arm. The system is studied at the beginning in the absence of controllers which resulted in poor results with great oscillation and overshoot in addition to a huge divergence from the expected reference. Three controllers for the three dimension reference forces were added but the results of two dimension forces ( $u_1, u_2$ ) continued having great oscillation and percentage of overshoot while the third ( $u_3$ ) converts to the anticipated outcome. With the introduction of PID controller into our study and refining its gain values the results began to convert towards the required results.

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